# Active vs. Passive Investing

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**DSS Aarhus** October 2017

# Active vs. passive: efficient vs. inefficient



 $\rightarrow$  a consistent theory of security markets and investment management

# **Overview of Talk**

Sharpening the arithmetic of active management

Efficiently in efficient markets for asset and asset management

The future of asset management



# Sharpe's "Arithmetic of Active Management"



**William Sharpe** Nobel Prize 1990

For illustrative purposes only. Image courtesy of http://www.nobelprize.org/nobel\_prizes/economic-sciences/laureates/1990/sharpe-bio.html

# Sharpe's "Arithmetic of Active Management"



For illustrative purposes only.

Image courtesy of http://www.nobelprize.org/nobel\_prizes/economic-sciences/laureates/1990/sharpe-bio.html

# **Investing vs. running**

If investing was like running a race

An above average investor would outperform the market, on average



For illustrative purposes only. Past performance is not a guarantee of future performance.

# Investing vs. running: if anyone can be average

If the worst investors use index funds and Sharpe's arithmetic holds

The investor who is just above average suddenly gets a below-average result

Sharpe's Arithmetic





For illustrative purposes only. Past performance is not a guarantee of future performance. Image on left courtesy of http://www.nobelprize.org/nobel\_prizes/economic-sciences/laureates/1990/sharpe-bio.html

# **Investing vs. running: asset managers**

### **Active management**

- Some investors benefit from the skills of managers
- But they pay a free

→ These effects make it even harder to perform well

# Sharpe's Arithmetic



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# **Investing vs. running: my arithmetic**

### **My Arithmetic**

### Sharpening the Arithmetic of Active Management

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Sharpe's (1991) famous "arithmetic of active management" states that

### "it must be the case that

 before costs, the return on the average actively managed dollar will equal the return on the average passively managed dollar, and

(2) after costs, the return on the average actively managed dollar will be less...

These assertions will hold for any time period. Moreover, they depend only on the laws of addition, subtraction, multiplication and division. Nothing else is required." [Emphasis in original]

Sharpe's arithmetic is often stated as incontrovertible fact by speakers at conferences followed by a triumphant "QEDI" and is cited as proof that active management is "doomed" in aggregate (French 2008).

If active management is doomed, then so is our marker-based financial system because we need someone to make prices informative. However, I show that Sharpe's equality does <u>not</u> hold in general. If is arithmetic is based on the implicit assumption that the marker portfolio never changes. When we relax this assumption, which does not hold in the real world, Sharpe's arithmetic is no longer a mathematical identity.

Sharpe's argument ignores a key aspect of addition and subtraction; namely the addition of new firms and shares and the subtraction of disappearing ones. Although seemingly minor; the market portfolio changes importantly over time such that even 'passive' investors must trade regularly, for instance to buy newly issued shares and sell those being repurchased. Whenever passive investors trade in order to maintain their market-weighted portfolios, they may trade at less favorable prices than active managers, which breaks charpe's equality.

This turnover of the market portfolio is important for two reasons. First, the changes of the market portfolio are large enough that active managers can potentially add noticeable returns relative to passive investors. Second, the issuance of securities is at the heart of a market-based conomy. When we put these reasons together, we see that active management can be worth positive fees, which in turn allows active managers to provide an important, beneficial role in the economy — helping to allocate resources efficiently.

Sharpe (1991 and 2013) is fighting a good and important fight in pointing out the importance of fees and the flaws of many arguments in favor of active management. I think that low-cost index funds is one



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# **Sharpening the Arithmetic of Active Management**

arithmetic



### **First Objection:**

- Informed (i.e. good) vs. uninformed (i.e., bad) managers
- Informed managers can outperform even if the average doesn't

### **Broader Objection:**

• Can you be passive by being inactive?

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# Even a "passive" investor must trade



The fraction of the market owned by an investor who starts off with the market portfolio but never trades after that (i.e., no participation in IPOs, SEOs, or share repurchases). Each line is a different starting date.

Source: Sharpening the Arithmetic of Active Management (Pedersen 2016). Shows path of an investor starting in a given year (1926, 1946, 1966, 1986, 2006) with the market portfolio and not trading thereafter. Market portfolio is all stocks included in the Center for Research in Security Prices (CRSP) database. For illustrative purposes only. Past performance is not a guarantee of future performance. Please read important disclosures in the Appendix.

# **Sharpening the Arithmetic of Active Management**

### Sharpe's hidden assumptions:

- Passive investors hold exactly the market
- The market never changes
- Passive investors trade to their market-cap weights for free

### These assumptions do not hold in the real world:

- IPOs, SEOs, share repurchases, etc.
- Index inclusions, deletions

### **Relaxing these assumption breaks Sharpe's equality**

- When passive investors trade, they may get worse prices
- Passive investors deviate from "true market"

### So active *can* be worth positive fees *in aggregate*

- Empirical questions:
  - Do they actually add value?
  - If so, how much? More than their fees?

### Fundamental economic issue, not a small "technical" issue

- Capital markets are about raising capital!
- The world is not a "pure exchange economy", the set of firms neither fixed nor "given"



Sharpe (1991 and 2013) is fighting a good and important fight in pointing out the importance of fees and the flaws of many arguments in favor of active management. I think that low-cost index funds is one

\* Copenhagen Business School, AQR Capital Management, NYU, and CEPR. I am grateful for helpful comments from Cliff Asness, Jatin Bhatia, Darrell Duffie, Jens Dick-Nielsen, Nicolae Garleanu, Niels Joachim Gormsen, Søren Hvidkjær, Antti Ilmanen, Ronen Israel, David Lando, John Liew, Toby Moskowitz, Lukasz Pomorski, Jesner Rangvid, Scott Richardson, William Sharpe, and Rodney Sullivan.



Sharpening the Arithmetic of Active Management

# Trading by a "passive" investor: Indices



### For S&P 500 and Russell 2000 (Petajisto, 2011)

- price impact from announcement to effective day has averaged
  - +8.8% and +4.7% for additions and -15.1% and -4.6% for deletions
- Iower bound of the index turnover cost:
  - 21–28 bp annually and 38–77 bp annually

Source: Sharpening the Arithmetic of Active Management (Pedersen 2016). Turnover from 1926-2015 for equity indices (S&P500 and Russell 2000) and corporate bond indices (BAML investment grade and high yield indices), and turnover is computed as sum of absolute changes in shares outstanding as a percentage of total market value in the previous month. "Other" includes mergers that may not require trading. For illustrative purposes only. Past performance is not a guarantee of future performance. Please read important disclosures in Appendix.

# **Sharpening the Arithmetic: Model**

- Passive investors buy
  - a fraction  $\boldsymbol{\theta}$  of each security  $\boldsymbol{i}$  included in their definition of the "market"
  - zero of each non-included security *n*
- Securities
  - Non-included securities are added to the market ("switch up") with probability  $s^u$
  - Included securities are deleted ("switch down") with probability  $s^d$
- Active investors
  - solve standard portfolio problem
- Equilibrium, closed-form solution
  - Active investors expect to outperform passive, before costs/fees
- Calibration
  - Outperformance of the order of institutional fees, smaller than typical retail fees

# Security markets vs. asset management markets

	Security markets	Asset management markets
Efficient	Fama (1970)	
Inefficient	Shiller (1980)	Fama (1970)

### **Definition: Efficiently inefficient markets**

- inefficient enough that active investors are compensated for their costs
- · efficient enough to discourage additional active investing

### Said differently:

- These markets must be difficult but not impossible to beat
- Grossman and Stiglitz (1980): "equilibrium degree of disequilibrium"

Source: Efficiently Inefficient (Pedersen 2015).

# Efficiently inefficient Markets for Assets and Asset Management

(Journal of Finance, forthcoming, with Nicolae Garleanu)



# **General Equilibrium for Assets and Asset Management**

### Solution

- Asset-market equilibrium as in Grossman-Stiglitz (1980), where inefficiency,  $\eta = \eta(A, M)$
- Asset management fee:  $f = \frac{\eta}{2\gamma}$
- (*A*, *M*) active investors and informed managers determined as 2 equations with 2 unknowns



# **Asset Management Frictions and Asset Prices**



# Proposition

- i. Lower search costs *c*:
  - More active investors A, more informed investors I, smaller price inefficiency  $\eta$ , lower fee f
  - Higher/lower *M* and total fee revenue

### ii. Vanishing search costs, $c \rightarrow 0$ :

- when c sufficiently low:  $A = \overline{A}$
- If  $\overline{A} \to \infty$ , then  $\eta \to 0$ ,  $f \to 0$ ,  $M \to 0$ , and the total fee revenue  $f(A + N) \to 0$  (full efficiency)

# **Efficiently inefficient Markets for Assets and Asset Management**

(Journal of Finance, forthcoming, with Nicolae Garleanu)

### Efficiently Inefficient Markets for Assets and Asset Management

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This version: September 2016

### Abstract

We consider a model where investors can invest directly or search for an asset manager, information about assets is costly, and managers charge an endogenous fee. The efficiency of asset prices is linked to the efficiency of the asset management market: if investors can find managers more easily, more money is allocated to active management, fees are lower, and asset prices are more efficient. Informed managers outperform after fees, uninformed managers underperform after fees, and the net performance of the average manager depends on the number of "noise allocators." Small investors should be passive, but large and sophisticated investors benefit from searching for informed active managers since their search cost is low relative to capital. Hence, managers with larger and more sophisticated investors are expected to outperform.

Keywords: asset pricing, market efficiency, asset management, search, information JEL Codes: D4, D53, D83, G02, G12, G14, G23, L10

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# **Efficiently inefficient: Security Markets**

### Several strategies have historically outperformed

• Value, momentum, quality, carry, low-risk

### Failure of the Law of One Price:

- Stocks: Siamese twin stock spreads
- Bonds: Off-the-run vs. on-the-run bonds
- FX: Covered interest-rate parity violations
- Credit: CDS-bond basis

### **Bigger anomalies when**

- Information costs for managers are high
- Search costs for investors are high

### **<u>Conclusion</u>**: Security markets are

- not fully efficient
- efficiently inefficient



# **Efficiently inefficient: Asset Managers**

### "Old consensus" in the academic literature:

• Active mutual funds have <u>no skill</u>: looks only at *average* manager, Jensen (1968), Fama (1970)

"New consensus" in the academic literature

• <u>Skill exists</u> among mutual funds and can be predicted: Fama and French (2010), Kosowski, Timmermann, Wermers, White (2006):

"we find that a sizable minority of managers pick stocks well enough to more than cover their costs. Moreover, the superior alphas of these managers persist"

• <u>Skill exists</u> among hedge funds: Fung, Hsieh, Naik, and Ramadorai (2008), Jagannathan, Malakhov, and Novikov (2010), Kosowski, Naik, and Teo (2007):

"top hedge fund performance cannot be explained by luck"

• <u>Skill exists</u> in private equity and VC:

Kaplan and Schoar (2005)

"we document substantial persistence in LBO and VC fund performance"

### Conclusion: asset management market is efficiently inefficient

Good managers exist, but picking them is difficult (requires recourses, manager selection team, due diligence, etc.)



# **Efficiently inefficient: Investors**

### Institutional investors outperform retail investors

• Gerakos, Linnainmaa, and Morse (2015)

"institutional funds earned annual market-adjusted returns of 108 basis points before fees and 61 basis points after fees"

### Larger pension funds outperform smaller ones

• Dyck and Pomorski (2015)

### Follow the smart money

• Evans and Fahlenbrach (2012)

*"retail funds with an institutional twin outperform other retail funds by 1.5% per year "* 

## **<u>Conclusion</u>**: efficiently inefficient investors

- Evidence that more sophisticated investors can perform better
- These educate themselves and spend resources picking managers



Sources: Gerakos, Joseph, Juhani T. Linnainmaa, and Adair Morse (2016), "Asset manager funds," working paper. Evans, Richard, and Rudiger Falhenbrach (2012), "Institutional Investors and Mutual Fund Governance: Evidence from Retail – Institutional Fund Twins". Dyck, Alexander, and Lukasz Pomorski (2015), "Investor Scale and Performance in Private Equity Investments" and (2011), "Is Bigger Better? Size and Performance in Pension Management." For illustrative purposes only. Past performance is not a guarantee of future performance. Market inefficiency: not "yes" or "no", but "how much"?

The market inefficiency ( $\eta$  in the model) can be linked to

- the proportional fee  $f^{\%}$
- relative risk aversion  $\gamma^R$

 $\eta = 2 f^{\%} \gamma^{R} = 2 \times 1\% \times 3 = 6\%$ 

Market inefficiency can also be expressed by the difference in squared SR by informed vs. uninformed investors

$$E(SR_i^2) - E(SR_i^2) \cong 2\eta = 0.12 = 0.53^2 - 0.4^2$$

# The future of asset management – doom?

### Implications of Sharpe's zero-sum arithmetic:

- Active loses to passive after fees
- Money flows passive  $\rightarrow$  markets less efficient
- Surprisingly active still loses
- · Eventually all money leaves active, sector is doomed

### What happens if everyone is passive?

### All IPOs successful regardless of price

• Everyone asks for their fraction of shares

### Initial result: boom in IPOs

### **Eventual result: doom**

- Opportunistic firms fail
- Equity market collapses
- People lose trust in financial system
- No firms can get funded
- Real economy falters



# The future of asset management – my arithmetic

### My arithmetic:

- Suppose active loses to passive after fees
- Money flows to passive  $\rightarrow$  markets less efficient
- Active becomes more profitable  $\rightarrow$  new equilibrium, no doom

### The future of asset management

- Passive will continue to grow, but towards a level<100%
- Active management will survive, pressure on performance and fees
- Consolidation of industry, systematic investing and FinTech will continue to grow

### Capital market is a positive-sum game

- Issuers can finance useful projects
- Passive investors get low-cost access to equity
- Active managers compensated for their information costs



# Conclusion

Asset market linked to market for asset management

These markets are efficiently inefficient

Active investing and market efficiency: real economic effects

# EFFICIENTLY INEFFICIENT

HOW SMART MONEY INVESTS & MARKET PRICES ARE DETERMINED



# Appendix

# Trading by a "passive" investor: Stocks and bonds



Source: Sharpening the Arithmetic of Active Management (Pedersen 2016). Turnover from 1926-2015 for all US listed stocks included in CRSP and the US municipal bonds, Treasury bonds, mortgage-related bonds, corporate debt, federal agency securities, and asset-backed securities, and turnover is computed as sum of absolute changes in shares outstanding as a percentage of total market value in the previous month. "Other" includes mergers that may not require trading. For illustrative purposes only. Past performance is not a guarantee of future performance. Please read important disclosures in Appendix.

# **Sharpening the arithmetic: Examples**

### Why can active managers outperform in aggregate?

### Example 0: informed active managers win at the expense of non-informational investors

- Behavioral biases
- Leverage constrained investors
- Pension plans hedging liabilities
- Central banks intervening

**Example 1: IPOs, SEOs, and repurchases** 

**Example 2: Index additions and deletions** 

**Example 3: Changes in the "market" and private assets** 

**Example 4: Rebalancing** 

Doggiyo	informed active
Passive	uninformed active

# **Sharpening the Arithmetic: Model**

- Securities
  - Risk free rate  $r^f$
  - A fraction *I* of all risky securities are included in passive investors' definition of the "market"
  - Non-included securities are added to the market ("switch up") with probability  $s^u$
  - Included securities are deleted ("switch down") with probability  $s^d$
  - No aggregate risk with changes in the market portfolio
  - Dividend payments,  $D = E_t (D_{t+1}^i)$
- Passive investors buy
  - a fraction  $\boldsymbol{\theta}$  of each included security  $\boldsymbol{i}$
  - zero of each non-included security *n*
- Active investors choose portfolio π

$$\max_{\pi} \pi' (E_t (D_{t+1} + P_{t+1}) - (1 + r^f) P_t) - \frac{\gamma}{2} \pi' \pi$$

To understand the last term, note that we are looking for steady state equilibrium,  $P_t = P$ , so

$$\bar{\gamma} \operatorname{Var}(D_{t+1} + P_{t+1}) = \bar{\gamma} \operatorname{Var}(D_{t+1}) = \bar{\gamma} \sigma^2 \operatorname{Id} =: \frac{\gamma}{2} \operatorname{Id}$$

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# **Equilibrium condition**

• Active investor's optimal portfolio

$$\pi = \frac{1}{\gamma} (E_t (D_{t+1} + P_{t+1}) - (1 + r^f) P_t)$$

- In equilibrium, active investors must choose a position of
  - $\pi^i = 1 \theta$  for included securities and
  - $\pi^n = 1$  for non-included securities
- Steady state equilibrium,  $P_t = P$ , given by

$$(1+r^f)P^i = D + P^i - s^d (P^i - P^n) - \gamma (1-\theta) (1+r^f)P^n = D + P^n + s^u (P^i - P^n) - \gamma$$

# **Equilibrium: Solution and comparative statics**

• Equilibrium price premium  $\Delta P = P^i - P^n$  given by

$$\Delta P = \frac{\gamma \theta}{r^f + s^d + s^u}$$

- Comparative statics
  - Price premium increases with  $\gamma$  and  $\theta$
  - Decreases with  $s^d$  and  $s^u$ 
    - For *return difference*, there are additional effects see below
- Equilibrium prices

$$P^{i} = \frac{D - \gamma(1 - \theta) - s^{d}\Delta P}{P^{n} = \frac{p^{f}}{D - \gamma + s^{u}\Delta P}} = P^{n} + \Delta P$$

# **Return properties – Dollar returns**

• Value change for included securities, in excess of risk free profit

$$\mathbf{R}_{t+1}^{i} = D_{t+1}^{i} + (1 - s^{d})P_{t+1}^{i} + s^{d}P_{t+1}^{n} - P_{t+1}^{i}(1 + r^{f})$$

• Expected value:

$$E_t(\boldsymbol{R}_{t+1}^i) = \boldsymbol{D} - s^d \Delta P - r^f P^i$$

• Value change for non-included securities

$$E_t(\boldsymbol{R}_{t+1}^n) = \boldsymbol{D} + s^u \Delta P - r^f P^n$$

• Difference only depends on risk aversion and size of passive portfolio

$$E_t(\mathbf{R}_{t+1}^n - \mathbf{R}_{t+1}^i) = (r^f + s^d + s^u)\Delta P = \gamma\theta$$

# **Return properties – percentage returns**

• Return on included securities, with relative premium given by  $x = \Delta P / P^n$ 

$$r_{t+1}^{i} = \frac{D_{t+1}^{i} + (1 - s^{d})P_{t+1}^{i} + s^{d}P_{t+1}^{i}/(1 + x)}{P_{t}^{i}} - 1$$

• Expected return, given dividend yield  $\delta_t = \frac{E_t(D_{t+1}^i)}{P_t^i}$  and price appreciation  $\mu_t = \frac{E_t(P_{t+1}^i)}{P_t^i}$ :

$$E_t(r_{t+1}^i) = \delta_t + (\mu_t - 1) - s^d \mu_t \frac{x}{1+x}$$

• Return on non-included securities

$$E_t(r_{t+1}^n) = \frac{D_{t+1}^n + (1 - s^u)P_{t+1}^n + s^u P_{t+1}^n (1 + x)}{P_t^n} - 1 = (1 + x)\delta_t + (\mu_t - 1) + s^u x\mu_t$$

• Note that in steady state  $\mu_t = 1$ 

# **Return differences – percentage returns**

Return difference between non-included and included securities

$$E_t(r_{t+1}^n - r_{t+1}^i) = x\left(\delta_t + \frac{s^d \mu_t}{1+x} + s^u \mu_t\right) = x\left(\delta_t + \frac{s^d}{1+x} + s^u\right)$$

- Positive due to dividend-yield effect, additions, and deletions
  - Comparative statics:
    - Increases in  $\delta_t$ ,  $s^d$ ,  $s^u$  for given x
    - But x is endogenous and decreases in  $s^d$ ,  $s^u$  (as discussed above) see example below
- Active investors hold
  - all of the non-included stocks and  $1 \theta$  of the non-included
  - the value-weighted fraction of non-included stocks in their portfolio is

$$f = \frac{(1-I)P^n}{(1-I)P^n + I\theta P^i} = \frac{1-I}{1-I + I\theta(1+x)}$$

• Return difference between active investor *a* and a passive (before fees)

$$E_t(r_{t+1}^a - r_{t+1}^i) = fE_t(r_{t+1}^n - r_{t+1}^i) = fx\left(\delta_t + \frac{s^d}{1+x} + s^u\right)$$

# Numerical example

- Securities
  - Risk-free rate  $r^f = 2\%$
  - Expected dividend D = 1
  - Half the securities are included I = 50%
  - The fraction of deletions is  $s^d = 2\%$ , the fraction of non-included that are added is  $s^u = 2\%$

### • Investors

- Passive investors buy  $\theta = 40\%$  of the included shares
- Active investors have a risk aversion corresponding to  $\gamma = 0.5$ 
  - chosen to have a reasonable dividend yield of around 3%

### • Equilibrium

- Price of included securities  $P^i = 31.7$
- Price of non-included securities  $P^n = 28.3$
- Dividend yield of included securities is  $\delta = 3.2\%$
- Price premium is x = 12%
- The expected return difference for non-included vs. included stocks is  $E_t(r_{t+1}^n r_{t+1}^i) = 0.82\%$
- Given that the active investors hold f = 60% of assets in non-included securities, the excess return of active relative to passive is  $E_t(r_{t+1}^a r_{t+1}^i) = 0.49\%$  (before fees).

# Active minus passive return vs. the size of passive investing



# Active minus passive return vs. the size of active investing



# Active minus passive return vs. frequency of additions and deletions

